PART 2

MECHANICS OF THE HUMAN BODY
2.1 INTRODUCTION

Over the past 100 years, the understanding of the thermal and mechanical properties of human tissues and the physics that governs biological processes has been greatly advanced by the utilization of fundamental engineering principles in the analysis of many biological heat and mass transfer applications. During the past decade, there has been an increasingly intense interest in bioheat transfer phenomena, with particular emphasis on therapeutic and diagnostic applications. Relying on advanced computational techniques, the development of complex mathematical models has greatly enhanced our ability to analyze various types of bioheat transfer process. The collaborations among physiologists, physicians, and engineers in the bioheat transfer field have resulted in improved treatment, preservation, and protection techniques for biological systems, including use of heat or cold treatments to destroy tumors and the protection of humans from extreme environmental conditions.

In this chapter we start with fundamental aspects of local blood tissue thermal interaction. Discussions on how the blood effect is modeled then follow. Different approaches to theoretically modeling the blood flow in the tissue are shown. In particular the assumptions and validity of several widely used continuum bioheat transfer equations are evaluated. Different techniques to measure temperature, thermophysical properties, and blood flow are then described. The final part of the chapter focuses on one of the medical applications of heat transfer, hyperthermia treatment for tumors.

2.2 FUNDAMENTAL ASPECTS OF BIOHEAT TRANSFER

One of the remarkable features of the human thermoregulatory system is that we can maintain a core temperature near 37°C over a wide range of environmental conditions and during thermal stress. The value of blood flow to the body varies over a wide range depending upon the need for its three primary functions:
1. Mass transfer in support of body metabolisms. Blood transports oxygen to the rest of the body and transports carbon dioxide and other waste from the cells.

2. Regulation of systemic blood pressure. The vascular system is a primary effector in the regulation of systemic blood pressure through its ability to alter the distribution of blood flow and regulate the cardiac output and thereby buffer systemic pressure fluctuations.


As for the third primary function, blood is known to have a dual influence on the thermal energy balance. First it can be a heat source or sink, depending on the local tissue temperature. During wintertime, blood is transported from the heart to warm the rest of the body. On the other hand, during hyperthermia treatment for certain diseases where the tissue temperature is elevated to as high as 45°C by external devices, the relatively cold blood forms cold tracks that can decrease the treatment efficacy. The second influence of the blood flow is that it can enhance heat dissipation from the inside of the body to the environment to maintain a normal body temperature. Theoretical study has shown that if the heat produced in the central areas of the body at rest condition could escape only by tissue conduction, the body temperature would not reach a steady state until it was about 80°C. A lethal temperature would be reached in only 3 hours. During exercise, our body temperature would typically rise 12°C in 1 hour if no heat were lost by blood flow. Maintaining a core temperature of 37°C during thermal stress or exercise is achieved by increasing the cardiac output by central and local thermoregulation, redistributing heat via the blood flow from the muscle tissue to the skin, and speeding the heat loss to the environment by evaporation of sweat.

Thermal interaction between blood and tissue can be studied either experimentally or theoretically. However, for the following reasons it is difficult to evaluate heat transfer in a biological system:

- The complexity of the vasculature. It is not practical to develop a comprehensive model that includes the effect of all thermally significant vessels in a tissue. Therefore, the most unusual and difficult basic problem of estimating heat transfer in living biologic systems is modeling the effect of blood circulation.
- Temperature response of the vasculature to external and internal effects is also a complex task. In a living system, the blood flow rate and the vessel size may change as a response to local temperature, local pH value, and the concentration of local O₂ and CO₂ levels.
- The small thermal length scale involved in the microvasculature. Thermally significant blood vessels are generally in a thermal scale of less than 300 µm. It has been difficult to build temperature-measuring devices with sufficient resolution to measure temperature fluctuation.

For the above reasons, even if the heat transfer function of the vascular system has been appreciated since the mid-nineteenth century, only in the past 2 decades, has there been a revolution in our understanding of how temperature is controlled at the local level, both in how local microvascular blood flow controls the local temperature field and how the local tissue temperature regulates local blood flow.

Until 1980, it was believed that, like gaseous transport, heat transfer took place in the capillaries because of their large exchange surface area. Several theoretical and experimental studies (Chato, 1980; Chen and Holmes, 1980; Weinbaum et al., 1984; Lemons et al., 1987) have been performed to illustrate how individual vessels participate in local heat transfer and thus, to understand where the actual heat transfer between blood and tissue occurs. In these analyses, the concept of thermal equilibration length was introduced. Thermal equilibration length of an individual blood vessel was defined as a distance over which the temperature difference between blood and tissue drops a certain percentage. For example if the axial variation of the tissue and blood temperature difference can be expressed as \( \Delta T = \Delta T_0 e^{-z/L} \), where \( \Delta T_0 \) is the temperature difference at the vessel entrance, then \( L \) and \( 4.6L \) are the thermal equilibration length over which \( \Delta T \) decreases to 37 percent and 1 percent, respectively, of its value at the entrance. Blood vessels whose thermal equilibration length is comparable to their physical length are considered thermally significant.
Chato (1980) first theoretically investigated the heat transfer from individual blood vessels in three configurations: a single vessel, two vessels in counterflow, and a single vessel near the skin surface. It was shown that the Graetz number, proportional to the blood flow velocity and radius, is the controlling parameter determining the thermal equilibration between the blood and tissue. For blood vessels with very low Graetz number, blood quickly reaches the tissue temperature. It was also demonstrated that heat transfer between the countercurrent artery and vein was affected by the vessel center-to-center spacing and mass transport between them.

In an anatomic study performed on rabbit limbs, Weinbaum et al. (1984) identified three vascular layers (deep, intermediate, and cutaneous) in the outer 1-cm tissue layer. Subsequently, three fundamental vascular structures were derived from the anatomic observation: (1) an isolated vessel embedded in a tissue cylinder, as shown by the intermediate tissue layer; (2) a large artery and its countercurrent vein oriented obliquely to the skin surface, as shown in the deep tissue layer; and (3) a vessel or vessel pair running parallel to the skin surface in the cutaneous plexus. These three vascular structures served as the basic heat transfer units in the thermal equilibration analysis in Weinbaum et al. (1984).

As shown in Weinbaum et al. (1984), 99 percent thermal equilibration length of a single blood vessel embedded in a tissue cylinder was derived as

\[
x_{cr} = 1.15a \text{Pr Re} \left[ 0.75 + K \ln \left( \frac{R}{a} \right) \right]
\]  

where \(a\) and \(R\) are the blood vessel and tissue cylinder radius, respectively, \(\text{Pr}\) and \(\text{Re}\) are the vessel Prandtl number and Reynolds number, respectively, and \(K\) is the ratio of blood conductivity to tissue conductivity. It is evident that \(x_{cr}\) is proportional to the blood vessel size and its blood flow velocity. Substituting the measured vascular geometry and the corresponding blood flow rate number for different blood vessel generations (sizes) from a 13-kg dog (Whitmore, 1968), one could calculate the thermal equilibration length as listed in Table 2.1.

<table>
<thead>
<tr>
<th>Vessel radius, (a, \mu m)</th>
<th>Vessel length, (L, cm)</th>
<th>(R/a)</th>
<th>(x_{cr}, cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>300</td>
<td>1.0</td>
<td>30</td>
<td>9.5</td>
</tr>
<tr>
<td>100</td>
<td>0.5</td>
<td>20</td>
<td>0.207</td>
</tr>
<tr>
<td>50</td>
<td>0.2</td>
<td>10</td>
<td>0.014</td>
</tr>
<tr>
<td>20</td>
<td>0.1</td>
<td>7</td>
<td>0.0006</td>
</tr>
</tbody>
</table>

Several conclusions were drawn from the comparison between \(x_{cr}\) and \(L\). In contrast to previous assumptions that heat transfer occurs in the capillary bed, for blood vessels smaller than 50 \(\mu m\) in diameter, blood quickly reaches the tissue temperature; thus, all blood-tissue heat transfer must have already occurred before entering into these vessels. For blood vessels larger than 300 \(\mu m\) in diameter, there is little change in blood temperature in the axial direction because of their much longer thermal equilibration length compared with the vessel length. The medium-size vessels between 50 and 300 \(\mu m\) diameter are considered thermally significant because of their comparable thermal equilibration length and physical length. Those blood vessels are primary contributors to tissue heat transfer. Note that the conclusions are similar to that drawn by Chato (1980).

The most important aspect of the bioheat transfer analysis by Weinbaum and coinvestigators was the identification of the importance of countercurrent heat transfer between closely spaced, paired arteries and veins. The countercurrent heat exchange mechanism, if dominant, was suggested as an energy conservation means since it provides a direct heat transfer path between the vessels. It was observed that virtually all the thermally significant vessels (>50 \(\mu m\) in diameter) in the skeletal muscle were closely juxtaposed artery-vein pairs (Weinbaum et al., 1984). Thermal equilibration in
the artery (50 to 300 µm diameter) in a countercurrent pair was estimated on the basis of a simple heat conduction analysis in the cross-sectional plane. It was noted that the thermal equilibration length in the countercurrent artery was at least 3 times shorter than that in a single vessel of the same size embedded in a tissue cylinder (Weinbaum et al., 1984). Significantly short thermal equilibration length in comparison with that of a single vessel suggests that the primary blood tissue heat exchange mechanism for vessels larger than 50 µm in the deep layer is the incomplete countercurrent heat exchange. Therefore, for modeling heat transfer in these tissue regions, reasonable assumptions related to the countercurrent heat exchange can be made to simplify the mathematical formulation.

Theoretical analysis of the thermal equilibration in a large vessel in the cutaneous layer (Chato, 1980; Weinbaum et al., 1984) demonstrated that its thermal equilibration length was much longer than its physical length during normal and hyperemic conditions despite the close distance from the skin surface. It was suggested that the large vessels in the cutaneous layer can be far from thermal equilibration and are therefore capable of delivering warm blood from the deep tissue to the skin layer. This superficial warm blood shunting is very important in increasing the normal temperature gradient at the skin surface and therefore plays an important role in losing heat during heavy exercise. On the contrary, during surface cooling there is rapid cutaneous vasoconstriction in the skin. The minimally perfused skin, along with the underlying subcutaneous fat, provides a layer of insulation, and the temperature gradient from the skin surface into the muscle becomes almost linear (Bazett, 1941) yielding the lowest possible heat transfer from the body.

2.3 BIOHEAT TRANSFER MODELING

The effects of blood flow on heat transfer in living tissue have been examined for more than a century, dating back to the experimental studies of Bernard in 1876. Since then, mathematical modeling of the complex thermal interaction between the vasculature and tissue has been a topic of interest for numerous physiologists, physicians, and engineers. A major problem for theoretical prediction of temperature distribution in tissue is the assessment of the effect of blood circulation, which is the dominant mode of heat removal and an important cause of tissue temperature inhomogeneity.

Because of the complexity of the vascular geometry, there are two theoretical approaches describing the effect of blood flow in a biological system. Each approach represents two length scales over which temperature variations may occur.

- **Continuum models**, in which the effect of blood flow in the region of interest is averaged over a control volume. Thus, in the considered tissue region, there is no blood vessel present; however, its effect is treated by either adding an additional term in the conduction equation for the tissue or changing some of the thermophysical parameters in the conduction equation. The continuum models are simple to use, since the detailed vascular geometry of the considered tissue region need not be known as long as one or two representative parameters related to blood flow are available. The shortcoming of the continuum model is that since the blood vessels disappear, no point-by-point variation in the blood temperature is available. Another shortcoming is associated with the assumptions introduced when the continuum model was derived. For different tissue regions and physiological conditions, these assumptions may not be valid.

- **Vascular models**, in which blood vessels are represented as tubes buried in tissue. Because of the complicated vascular geometry, one may only consider several blood vessels and neglect the others. Recent studies [Dorr and Hynynen, 1992; Crezee and Lagendijk, 1990; Roemer, 1990] have demonstrated that blood flow in large, thermally unequilibrated vessels is the main cause for temperature nonhomogeneity during hyperthermia treatment. Large blood vessels may significantly cool tissue volumes around them, making it very difficult to cover the whole tumor volume with therapeutic thermal exposure. In applications where point-to-point temperature
nonuniformities are important, vascular model has been proved to be necessary to predict accurately the tissue temperature field (Zhu et al., 1996a). In recent years, with the breakthrough of advanced computational techniques, vascular models [Raaymakers et al., 2000] for simulating vascular networks have grown rapidly and already demonstrated its great potential in accurate and point-to-point blood and tissue temperature mapping.

2.3.1 Continuum Models

In continuum models, blood vessels are not modeled individually. Instead, the traditional heat conduction equation for the tissue region is modified by either adding an additional term or altering some of the key parameters. The modification is relatively simple and is closely related to the local vasculature and blood perfusion. Even if the continuum models cannot describe the point-by-point temperature variation in the vicinity of larger blood vessels, they are easy to use and allow the manipulation of one or several free parameters. Thus, they have much wider applications than the vascular models. In the following sections, some of the widely used continuum models are introduced and their validity is evaluated on the basis of the fundamental heat transfer aspects.

Pennes Bioheat Transfer Model. It is known that one of the primary functions of blood flow in a biological system is its ability to heat or cool the tissue, depending on the relative local tissue temperature. The existence of a temperature difference between the blood and tissue is taken as evidence of its function to remove or release heat. On the basis of this speculation, Pennes [Pennes, 1948] proposed his famous bioheat transfer model, which is called Pennes’ bioheat equation. Pennes suggested that the effect of blood flow in the tissue be modeled as as heat source or sink term added to the traditional heat conduction equation. The Pennes bioheat equation is given by

\[ \rho C \frac{\partial T}{\partial t} = k \nabla^2 T + q_{\text{blood}} + q_m \]  

(2.2)

where \( q_m \) is the metabolic heat generation in the tissue and the second term (\( q_{\text{blood}} \)) on the right side of the equation takes into account the contribution of blood flow to the local tissue temperature distribution. The strength of the perfusion source term can be derived as follows.

Figure 2.1 shows a schematic diagram of a small tissue volume perfused by a single artery and vein pair. The tissue region is perfused via a capillary network bifurcated from the transverse arterioles, and the blood is drained by the transverse venules. If one assumes that both the artery and
vein keep a constant temperature when they pass through this tissue region, the total heat released is equal to the total amount of blood perfusing this tissue volume \( q \) multiplied by its density \( \rho_b \) specific heat \( C_b \), and the temperature difference between the artery and vein, and is given by

\[
q\rho_b C_b (T_a - T_v) = (Q_{in} - Q_{out})\rho_b C_b (T_a - T_v)
\]

(2.3)

The volumetric heat generation rate \( q_{\text{blood}} \), defined as the heat generation rate per unit tissue volume, is then derived as

\[
q_{\text{blood}} = \omega \rho_b C_b (T_a - T_v)
\]

(2.4)

where \( \omega \) is defined as the amount of blood perfused per unit volume tissue per second.

Note that both \( T_a \) and \( T_v \) in Eq. (2.4) are unknown. Applying the analogy with gaseous exchange in living tissue, Pennes believed that heat transfer occurred in the capillaries because of their large area for exchange. Thus, the local arterial temperature \( T_a \) could be assumed as a constant and equal to the body core temperature \( T_c \). As for the local venous blood, it seems reasonable to assume that it equilibrates with the tissue in the capillary and enters the venules at the local tissue temperature. Then the Pennes bioheat equation becomes

\[
\rho C \frac{\partial T}{\partial t} = k \nabla^2 T + \omega \rho_b C_b (T_c - T_v) + q_m
\]

(2.5)

This is a partial differential equation for the tissue temperature. As long as an appropriate initial condition and boundary conditions are prescribed, the transient and steady-state temperature field in the tissue can be determined.

The limitations of the Pennes equation come from the basic assumptions introduced in this model. First it is assumed that the temperature of the arterial blood does not change when it travels from the heart to the capillary bed. As shown in Sec. 2.2, small temperature variations occur only in blood vessels with a diameter larger than 300 \( \mu m \). Another assumption is that the venous blood temperature is approximated by the local tissue temperature. This is valid only for blood vessels with a diameter smaller than 50 \( \mu m \). Thus, without considering the thermal equilibration in the artery and vein in different vessel generations, the Pennes source term obviously overestimates the effect of blood perfusion. To accurately model the effect of blood perfusion, the temperature variation along the artery and the heat recaptured by the countercurrent vein must be taken into consideration.

Despite the limitations of the Pennes bioheat equation, reasonable agreement between theory and experiment has been obtained for the measured temperature profiles in perfused tissue subject to various heating protocols. This equation is relatively easy to use, and it allows the manipulation of two blood-related parameters, the volumetric perfusion rate and the local arterial temperature, to modify the results. Pennes performed a series of experimental studies to validate his model. Over the years, the validity of the Pennes bioheat equation has been largely based on macroscopic thermal clearance measurements in which the adjustable free parameter in the theory, the blood perfusion rate \([Xu and Anderson, 1999]\) was chosen to provide reasonable agreement with experiments for the temperature decay in the vicinity of the thermistor bead probe. Indeed, if the limitation of Pennes’ bioheat equation is an inaccurate estimation of the strength of the perfusion source term, an adjustable blood perfusion rate will overcome its limitations and provide reasonable agreement between experiment and theory.

**Weinbaum-Jiji Bioheat Equation.** Since 1980, researchers (Chen and Holmes, 1980; Chato, 1980; Weinbaum et al., 1984) have begun to question the validity of the Pennes bioheat equation. Later, Weinbaum and Jiji (1985) developed a new equation for microvascular blood tissue heat transfer, based on the anatomic analysis (Weinbaum et al., 1984), that illustrated that the predominant mode of heat transfer in the tissue was the countercurrent heat exchange between a thermally significant artery and vein pair. The near-perfect countercurrent heat exchange mechanism implies that most of the heat leaving the artery is transferred to its countercurrent vein rather than released to the surrounding tissue. Once there is a tissue temperature gradient along the countercurrent vessel axes, the artery and
vein will transfer a different amount of energy across a plane perpendicular to their axes even if there is no net mass flow. This gives rise to a net energy transfer that is equivalent to an enhancement in tissue conductivity in the axial direction of the vessels. In the Weinbaum-Jiji equation, the thermal effect of the blood perfusion is described by an enhancement in thermal conductivity $k_{\text{eff}}$, appearing in the traditional heat conduction equation,

$$\rho C \frac{\partial T}{\partial t} = k_{\text{eff}} \nabla^2 T + q_m \quad k_{\text{eff}} = k[1 + f(\omega)] \quad (2.6)$$

It was shown that $k_{\text{eff}}$ is a function of the local blood perfusion rate and local vascular geometry.

The main limitations of the Weinbaum-Jiji equation are associated with the importance of the countercurrent heat exchange. It was derived to describe heat transfer in peripheral tissue only, where its fundamental assumptions are most applicable. In tissue area containing a big blood vessel (>200 µm in diameter), the assumption that most of the heat leaving the artery is recaptured by its countercurrent vein could be violated, thus, it is not an accurate model to predict the temperature field. In addition, this theory was primarily developed for closely paired microvessels in muscle tissue, which may not always be the main vascular structure in other tissues, such as the renal cortex. Furthermore, unlike the Pennes equation, which requires only the value of blood perfusion, the estimation of the enhancement in thermal conductivity requires that detailed anatomical studies be performed to estimate the vessel number density, size, and artery-vein spacing for each vessel generation, as well as the blood perfusion rate (Zhu et al., 1995). These anatomic data are normally not available for most blood vessels in the thermally significant range.

**A New Modified Bioheat Equation.** The Pennes and Weinbaum-Jiji models represent two extreme situations of blood-vessel thermal interaction. In the original Pennes model, the arterial blood releases all of its heat to the surrounding tissue in the capillaries and there is no venous rewarming. Pennes did not realize that thermal equilibration was achieved in vessels at least an order of magnitude larger than the capillaries. In contrast, in the Weinbaum-Jiji model the partial counter-current rewarming is assumed to be the main mechanism for blood-tissue heat transfer. The derivation of the Weinbaum-Jiji equation is based on the assumption that the heat transfer between the artery and the vein does not depart significantly from a perfect countercurrent heat exchanger. In other words, most of the heat lost by the artery is recaptured by its countercurrent vein rather than lost to the surrounding tissue. Subsequent theoretical and experimental studies have shown this is a valid assumption only for vessels less than 200 µm diameter (Charny et al., 1990; Zhu et al., 1996a).

Several theoretical studies have suggested that one way to overcome the shortcomings of both models was to introduce a “correction coefficient” in the Pennes perfusion term [Chato, 1980; Baish, 1994; Brinck and Werner, 1994; Weinbaum et al., 1997; Zhu et al., 2002]. In 1997, Weinbaum and coworkers (Weinbaum et al., 1997) modified the Pennes source term on the basis of the thermal analysis of a basic heat transfer unit of muscle tissue, a 1-mm-diameter tissue cylinder containing blood vessels smaller than 200 µm in diameter [Fig. 2.2]. The countercurrent heat exchange between the artery and vein defined in the anatomical studies of Myrhage and Eriksson [1984] led to the estimation of the heat loss recaptured by the vein. The strength of the source term was then rederived taking into account the rewarming of the countercurrent venous blood in the tissue cylinder. The thermal equilibration analysis on the countercurrent artery and vein in the tissue cylinder led to the following bioheat transfer equation:

$$\rho C \frac{\partial T}{\partial t} = k_{\text{eff}} \nabla^2 T + \epsilon \omega p_b C_s (T_{\text{ave}} - T) + q_m \quad (2.7)$$

Note that the only modification to the Pennes model is a correction coefficient $\epsilon$ in the Pennes source term. This coefficient can be viewed as a weighting function to correct the overestimation of the original Pennes perfusion term. An easy-to-use closed-form analytic expression was derived for
2.10 MECHANICS OF THE HUMAN BODY

this coefficient that depends on the vessel spacing and radius. From the anatomic studies of the vascular arrangements of various skeletal muscles, the correction coefficient was found to vary from 0.6 to 0.8 under normal physiological conditions, indicating that there is a 20 to 40 percent rewarming of the countercurrent vein. Note that it is close to neither unity (the Pennes model) nor zero (the Weinbaum-Jiji model). Thus, both the Pennes and the Weinbaum-Jiji equation are not valid for most muscle tissue. Furthermore, as shown in Zhu et al. (2002), the arterial temperature \( T_{a0} \) may not be approximated as the body core temperature unless the local blood perfusion is very high. In most physiological conditions, it is a function of the tissue depth, blood vessel bifurcation pattern, and the local blood perfusion rate.

2.3.2 Experimental and Theoretical Studies to Validate the Models

Pennes (1948) performed a series of experimental studies to validate his model. He inserted and pulled thermocouples through the arms of nine male subjects to measure the radial temperature profiles. He also measured the skin temperature distributions along the axis of the upper limb, as well as around the circumference of the forearm. Pennes then modeled the arm as a long cylinder and calculated the steady-state radial temperature profile. In this theoretical prediction, since the blood perfusion rate \( \omega \) could not be directly measured, Pennes adjusted this parameter in his model to fit the solution to his experimental data for a fixed, representative ambient temperature and metabolic heating rate. The fitted value of blood perfusion rate \( \omega \) was found to be between 1.2 and 1.8 mL blood/min/100g tissue, which is a typical range of values for resting human skeletal muscle. Recently, Wissler [1998] re-evaluated Pennes’ original paper and analyzed his data. He found that the theoretical prediction agrees very well with Pennes’ experimental results if the data were analyzed in a more rigorous manner.

Profound understanding of the heat transfer site and the countercurrent heat exchange between paired significant vessels was gained through the experiments [Lemons et al., 1987] performed on...
rabbit thigh to measure the transverse temperature profiles in the rabbit thigh using fine thermocouples. The experimental study was designed to achieve two objectives. The first is to examine whether there exists detectable temperature difference between tissue and blood for different-size vessels. Existing detectable blood-tissue temperature difference implies that blood has not reached thermal equilibration with the surrounding tissue. The second is to examine the temperature difference between the countercurrent artery and vein. If the countercurrent heat exchange is dominant in blood tissue heat transfer, the vein must recapture most of the heat leaving the artery; thus, the temperature difference between the countercurrent artery and vein should not vary significantly in the axial direction.

Experimental measurements (Lemons et al., 1987) revealed small temperature fluctuations of up to 0.5°C in the deep tissue. The irregularities in the tissue temperature profiles were closely associated with the existence of blood vessels in the vicinity of the thermocouple wire. It was shown that temperature fluctuation was observed in all the blood vessels larger than 500 µm, in 67 percent of the vessels between 300 and 500 µm, and in 9 percent of the vessels between 100 and 300 µm. No temperature fluctuation was observed in blood vessels less than 100 µm in diameter. This finding indicates that the assumption in the Pennes model that arterial blood reaches the capillary circulation without significant prior thermal equilibration is inaccurate for this vascular architecture, and thus most of the significant blood-tissue heat transfer occurs in the larger vessels upstream. It was also observed that the temperature field rarely exceeded 0.2°C in any countercurrent pair, even when the difference in temperature between the skin and the central part of the rabbit thigh exceeded 10°C. This implies the effectiveness of the countercurrent heat exchange process throughout the vascular tree.

In a series of experiments with an isolated perfused bovine kidney, Crezee and Lagendijk (1990) inserted a small plastic tube into the tissue of a bovine kidney and measured the disturbance temperature fields in a plane perpendicular to the tube while heated water was circulated through it, and the kidney cortex was perfused at different rates. They also used thermocouples to map the temperature distribution in the tissue of isolated perfused bovine tongues at various perfusion rates (Crezee et al., 1991). By examining the effect of increased perfusion on the amplitude and width of the thermal profile, they demonstrated that the temperature measurements agreed better with a perfusion-enhanced $k_{eff}$ as opposed to the perfusion source term in the Pennes equation.

Charny (Charny et al., 1990) developed a detailed one-dimensional (1-D) three-equation model. Since this model was based on energy conservation and no other assumptions were introduced to simplify the analysis of the blood flow effect, it was viewed as a relatively more accurate model than both the Pennes and Weinbaum-Jiji equation. The validity of the assumptions inherent in the formulation of the Weinbaum-Jiji equation were tested numerically under different physiological conditions. In addition, the temperature profile predicted by the Pennes model was compared with that by the three-equation model and the difference between them was evaluated. The numerical simulation of the axial temperature distribution in the limb showed that the Weinbaum-Jiji equation provided very good agreement with the three-equation model for downstream vascular generations that are located in the outer layer in the limb muscle, while the Pennes model yielded better description of heat transfer in the upstream vessel generations. Considering that vessels bifurcate from approximately 1000 µm in the first generation to 150 µm in the last generation, one finds that the Pennes source term, which was originally intended to represent an isotropic heat source in the capillaries, is shown to describe instead the heat transfer from the largest countercurrent vessels, >500 µm in diameter. The authors concluded that this was largely attributed to the capillary bleedoff from the large vessels in these tissue regions. The capillary bleedoff appeared to result in a heat source type of behavior that matches the Pennes perfusion term. The Weinbaum-Jiji model, on the other hand significantly overestimated the countercurrent heat exchange in the tissue region containing larger blood vessels. The validity of the Weinbaum-Jiji equation requires that the ratio of the thermal equilibration length $L_e$ of the blood vessel to its physical length $L$ be less than 0.2. This criterion was found to be satisfied for blood vessels less than 300 µm in diameter under normothermic conditions.
2.12 MECHANICS OF THE HUMAN BODY

2.4 TEMPERATURE, THERMAL PROPERTY, AND BLOOD FLOW MEASUREMENTS

2.4.1 Temperature

The control of human body temperature is a complex mechanism involving hormones, blood flow to the skin, respiration, and metabolic rate. The control mechanism can be altered by certain pathologic (fever) and external (hyperthermia treatment) events. Consequently, temperature is an important parameter in the diagnosis and treatment for many disease. Elevated local temperature can be an indication of excess or abnormal metabolic rates. Inflammation is the body’s mechanism for removing foreign or diseased substances. Exercise also induces an increase in local temperature of skeletal muscles and joints. Some diagnostic procedures involve the measurement of temperature. Thermal images of the breasts have been used to detect the presence of malignant tumors. Temperature measurement is also critical in many therapeutic procedures involved in either hyperthermia or hypothermia.

Temperature-measuring devices can fall into two categories, invasive and noninvasive. Invasive temperature sensors offer the advantages of small size, fast response time, extreme sensitivity to temperature changes, and high stability. However, they have generally involved a limited number of measurement locations, uncertainties about the anatomic placement of thermometry devices, interaction with the energy applied, periodic rather than continuous temperature measurements, and, in some cases, surgical exposure of the target tissue for placement of the temperature probes.

Invasive temperature devices include thermocouples, thermistor beads, optical fiber sensors, etc. A thermocouple consists of two pieces of dissimilar metal that form two junctions. In the wire, an electric potential difference is formed if there exists a temperature difference between the two junctions. This potential difference can be measured with a voltmeter and translated to temperature with a fairly simple means of calibration. A thermocouple usually has a good long-term stability, responds very quickly to changes in temperature, and can be constructed in a manner that allows a good resolution. Another kind of invasive device, the thermistor bead, is made by depositing a small quantity of semiconductor paste onto closely spaced metal wires. The wire and beads are sintered at a high temperature when the material forms a tight bond. The wires are then coated with glass or epoxy for protection and stabilization. The resistors generally exhibit high thermal sensitivity. This characteristic sensitivity to temperature change can result in a thermistor resistance change of more than 50 °C. Unlike a thermocouple or thermistor bead, the fiber optic temperature probe does not interfere with an electromagnetic field. It has been used to measure tissue temperature rise induced by microwave and/or radio-frequency heating [Zhu et al., 1996b; 1998]. However, it is relatively big in size (~1.5 mm diameter) and has a lower temperature resolution (~0.2°C).

Noninvasive temperature-measuring techniques include MRI thermometry, infrared thermography, etc. Because of the theoretical sensitivity of some of its parameters to temperature, MRI has been considered to be a potential noninvasive method of mapping temperature changes during therapies using various forms of hyperthermia. MRI imaging has the advantage of producing three-dimensional anatomic images of any part of the body in any orientation. In clinical practice, MRI characteristic parameters such as the molecular diffusion coefficient of water, the proton spin-lattice (T1) relaxation time (Parker et al., 1982), and the temperature-dependent proton resonance frequency (PRF) shift have been used to estimate the in vivo temperature distribution in tissues. MRI provides good spatial localization and sufficient temperature sensitivity. At the present time, it also appears to be the most promising modality to conduct basic assessments of heating systems and techniques. The disadvantages of MRI thermometry include limited temporal resolution (i.e., quasi-real time), high environmental sensitivity, high material expenditure, and high running costs.

Infrared thermography is based on Planck’s distribution law describing the relationship between the emissive power and the temperature of a blackbody surface. The total radiative energy emitted by an object can be found by integrating the Planck equation for all wavelengths. This integration gives the Stefan-Boltzmann law \( E(T) = \epsilon \sigma T^4 \). The thermal spectrum as observed by an infrared-sensitive...
detector can be formed primarily by the emitted light. Hence, the formed thermal image is determined by the local surface temperature and the emissivity of the surface. If the emissivity of the object is known, and no intervening attenuating medium exists, the surface temperature can be quantified. Quantification of skin temperature is possible because the human skin is almost a perfect blackbody ($\epsilon = 0.98$) over the wavelengths of interest. Qualitative thermography has been successfully used in a wide range of medical applications (Jones, 1998) including cardiovascular surgery (Fiorini et al., 1982), breast cancer diagnoses (Gautherie and Gros, 1980; Lapayowker and Revesz, 1980), tumor hyperthermia (Cetas et al., 1980), laser angioplasty, and peripheral venous disease. Clinical studies on patients who had breast thermography demonstrated that an abnormal thermography was associated with an increased risk of breast cancer and a poorer prognosis for the breast cancer patients (Gautherie and Gros, 1980; Head et al., 1993). Infrared tympanic thermometry has also been developed and widely used in clinical practice and thermoregulatory research as a simple and rapid device to estimate the body core temperature (Matsukawa et al., 1996; Shibasaki et al., 1998).

2.4.2 Thermal Property (Thermal Conductivity and Thermal Diffusivity) Measurements

A knowledge of thermal properties of biological tissues is fundamental to understanding heat transfer processes in the biological system. This knowledge has increased importance in view of the concerns for radiological safety with microwave and ultrasound irradiation, and with the renewed interest in local and regional hyperthermia as a cancer therapy. The availability of a technique capable of accurately characterizing thermal properties of both diseased and normal tissue would greatly enhance diagnostic and therapeutic medicine.

The primary requirement in designing an apparatus to measure thermal conductivity and diffusivity is that the total energy supplied should be used to establish the observed temperature distribution within the specimen. For accurate measurements, a number of structural and environmental factors, such as undesired heat conduction to or from the specimen, convection currents caused by temperature-induced density variations, and thermal radiation, must be minimized. Biomaterials present additional difficulties. The existing literature on biological heat transfer bears convincing evidence of the complexity of heat transfer processes in living tissue. For example, thermal properties of living tissue differ from those of excised tissue. Clearly the presence of blood perfusion is a major factor in this difference. Relatively large differences in thermal conductivity exist between similar tissues and organs, and variation for the same organ, are frequently reported. Such variations suggest the importance of both defining the measurement conditions and establishing a reliable measurement technique.

The thermal property measurement techniques can be categorized as steady-state methods and transient methods. They can also be categorized as invasive and noninvasive techniques. In the following sections, we will focus on several widely used techniques for measuring tissue thermal conductivity or diffusivity. Their advantages and limitations will also be described.

**Guarded Hot Plate.** Thermal conductivity can be measured directly by using steady-state methods, such as the guarded hot plate. This method is invasive in that it requires the excision of the specimen for in vitro measurement. It typically involves imposing a constant heat flux through a specimen and measuring the temperature profile at specific points in the specimen after a steady-state temperature field has been established. Once a simple one-dimensional steady-state temperature field is established in the specimen, the thermal conductivity may be easily found by the expression

$$k = \frac{q'' L}{T_1 - T_2}$$

(2.8)

where $q''$ is the heat flux passing through the specimen, $T_1$ and $T_2$ are temperature values at any two measurement locations in the axial direction (or the direction of the heat flux), and $L$ is the axial distance between these two temperature measurements.
Biological materials typically have moderate thermal conductivities and therefore require extensive insulation to ensure an unidirectional heat flow. The contact resistance between the specimen and the plate is also difficult to be minimized. In addition, this method cannot be used to obtain in vivo measurements. Once the tissue specimen is cut from the body, dehydration and temperature-dependent properties may need to be considered.

**Flash Method.** The transient flash method, first proposed by Parker et al. (1961), is the current standard for measuring the thermal diffusivity of solids. A schematic diagram of this method is shown in Fig. 2.3. The front face of a thin opaque solid, of uniform thickness, is exposed to a burst of intense radiant energy by either a high-energy flash tube or laser. The method assumes that the burst of energy is absorbed instantaneously by a thin layer at the surface of the specimen. Adiabatic boundary conditions are assumed on all other surfaces and on the front face during the measurement. The transient temperature at the rear surface is then measured by using thermocouples or an infrared detector.

![Schematic diagram of a flash apparatus for sample diffusivity measurements.](image)

An analytic expression for the rear surface temperature transient is given by

$$T(l, t) - T(l, 0) = \frac{Q}{\rho Cl} \left[ 1 + 2 \sum_{n=1}^{\infty} (-1)^n \exp \left( -\frac{n^2 \pi^2}{l^2} \alpha t \right) \right]$$  \hspace{1cm} (2.9)

where $Q = $ absorbed radiant energy per unit area
- $\rho$ = mass density
- $C$ = specific heat
- $l$ = sample thickness
- $\alpha$ = thermal diffusivity

The maximum temperature at the rear surface is determined by the volumetric heating as $T_{\text{max}} = T(l, 0) + Q/\rho Cl$. The thermal diffusivity in the direction of heat flow is usually calculated by the expression

$$\alpha = 1.38 \frac{l^2}{\pi^2 t_{1/2}}$$  \hspace{1cm} (2.10)

where $t_{1/2}$ is the time required for the rear surface to reach half of its maximum temperature.

The simplicity of the method described above is often offset by the difficulty in satisfying the required adiabatic boundary conditions. In order for this solution to be valid, the radiant energy incident on the front surface is required to be uniform, and the duration of the flash must be sufficiently short compared with the thermal characteristic time of the sample. In addition, it assumes that the sample is homogeneous, isotropic, and opaque, and that the thermal properties of the sample do not vary considerably with temperature.
**Temperature Pulse Decay (TPD) Technique.** Temperature pulse decay (TPD) technique is based on the approach described and developed by Arkin, Chen, and Holmes [Arkins et al., 1986; 1987]. This method needs no insulation, in contrast to some of the methods described above, since testing times are short, usually on the order of seconds. However, the determination of the thermal conductivity or the blood flow rate requires the solution of the transient bioheat transfer equation.

This technique employs a single thermistor serving as both a temperature sensor and a heater. Typically in this technique, either a thermistor is inserted through the lumen of a hypodermic needle, which is in turn inserted into the tissue, or the thermistor is embedded in a glass-fiber-reinforced epoxy shaft. Figure 2.4 shows the structure of a thermistor bead probe embedded in an epoxy shaft. Each probe can consist of one or two small thermistor beads situated at the end or near the middle of the epoxy shaft. The diameter of the finished probe is typically 0.3 mm, and the length can vary as desired. Because the end can be sharpened to a point, it is capable of piercing most tissues with very minimal trauma.

![Sketch of a thermistor bead probe](FIGURE 2.4)

During the experiment, a short heating pulse of approximately 3 seconds is delivered by the thermistor bead. The pulse heating results in a temperature rise in the area near the tip of the probe. After the pulse heating, the temperature of the probe will decrease. During the pulse heating and its subsequent temperature decay, the temperature at the tip of the probe is measured by the thermistor bead. To determine the thermal conductivity or blood flow rate, a theoretical prediction of the transient temperature profile is needed for the same tissue domain as in the experimental study. Typically, the theoretically predicted temperature profile is obtained by solving a bioheat transfer equation in which the blood flow rate and thermal conductivity have to be given as input to the model. The predicted temperature profile is then compared with the experimental measurements. The values of the blood flow rate and/or thermal conductivity will be adjusted to minimize the square difference between the predicted temperature profile and the experimental measurements using the
linear-square residual fit. The values for the blood flow rate and thermal conductivity that give the best fit of the experimentally measured temperature profile are the calculated blood flow rate and thermal conductivity of the tissue sample.

Typically, the Pennes bioheat transfer equation is used to predict the temperature transient. It is assumed that the thermistor bead is small enough to be considered a point source inserted into the center of an infinitively large medium. The governing equation and initial condition for this thermal process are described as

\[ \rho C \frac{\partial T}{\partial t} = k \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial T}{\partial r} \right) + \omega \rho C (T_a - T_r) + q_p \]  

(2.11)

where \( q_p \) is the pulse heating deposited locally into the tissue through a very small thermistor bead probe; \( q_p = P \delta(0) \) for \( t \leq t_p \), \( q_p = 0 \) for \( t > t_p \). \( P \) is the deposited power, and \( \delta(0) \) is the Dirac delta function. Before the measurement, the steady-state temperature distribution \( T_{ss}(r) \) in the sample should satisfy the one-dimensional steady-state conduction equation without the pulse heating. The governing equation for \( T_{ss}(r) \) is given by

\[ 0 = k \frac{1}{r} \frac{d}{dr} \left( r \frac{dT_{ss}}{dr} \right) + \omega \rho C (T_a - T_{ss}) \]  

(2.12)

Subtracting Eq. (2.14) from Eq. (2.13), and introducing \( \theta = T - T_{ss} \), one obtains

\[ \rho C \frac{\partial \theta}{\partial t} = k \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial \theta}{\partial r} \right) + \omega \rho C \theta + q_p \]  

(2.13)

\[ t = 0 \quad \theta = 0 \]

For the limiting case of an infinitesimally small probe with an infinitesimally short heating pulse, the solution for Eq. (2.15) for the interval of temperature decay takes the form:

\[ \theta = \lambda_2 \int_0^r (t - s)^{-1.5} e^{-\omega(t-s)} e^{-2/\lambda_1(t-s)} ds \]  

(2.14)

where \( \lambda_1 = P(\rho C)^{0.5/(8\pi^{1.5})} \) and \( \lambda_2 = \omega/(k^{1.5}r^{0.5}) \). In this theoretical analysis, there are two unknowns, \( k \) and \( \omega \). A least squares residual fit allows one to find a set of values of \( k \) and \( \omega \) that will lead to the best fit of the theoretical predictions to the experimentally measured temperature decay.

The temperature pulse decay technique has been used to measure both the in vivo and in vitro thermal conductivity and blood flow rate in various tissues (Xu et al., 1991; 1998). The specimen does not need to be cut from the body, and this method minimizes the trauma by sensing the temperature with a very small thermistor bead. For the in vitro experimental measurement, the measurement of thermal conductivity is simple and relatively accurate. The infinitively large tissue area surrounding the probe implies that the area affected by the pulse heating is very small in comparison with the tissue region. This technique also requires that the temperature distribution before the pulse heating should reach steady state in the surrounding area of the probe.

### 2.4.3 Blood Perfusion Measurement

Blood perfusion rate is defined as the amount of blood supplied to a certain tissue region per minute per 100 g tissue weight. In most of the situation, it is representing the nutrient need in that tissue area. High blood perfusion is also associated with heat dissipation during exercise or thermal stress. In humans, there are several tissue regions, such as kidney, heart, and choriocapillaris in the eye,
possessing a high blood perfusion rate. The measured blood perfusion rate in the kidney is approximately 500 mL/min/100 g tissue (Holmes, 1997). In the heart, the blood perfusion rate is around 300 mL/min/100 g, which serves for the energy need of pumping the heart. The choriocapillaris in the eyes is a meshed structure within two thin sheets. Its blood perfusion rate is very high and can be as much as 8000 mL/min/100 g tissue. In addition to providing oxygen and other nutrients to the retina, the choriocapillaris also may play a role in stabilizing the temperature environment of the retina and retinal pigment epithelium (Aurer and Carpenter, 1980). In addition to its physiological role, blood perfusion measurement is important in theoretical modeling of the temperature distribution during various therapeutic and diagnostic applications.

**Radiolabeled Microsphere Technique.** Measurement of blood flow has become an integral part of the physiologic study of humans. While many methods have been utilized in measuring tissue blood flow, the one most often practiced today is dependent on injection of radioactively labeled microspheres. The reason for its overwhelming acceptance is due, in part, to the shortcomings of many of the alternative methods of blood flow determination.

In principle, small particles are uniformly mixed with blood and allowed to circulate freely until they impact in a vessel smaller in diameter than themselves. The tissue or organ is then removed and its radioactivity measured. In such a system, the number of particles impacted in a given tissue is assumed proportional to the volume of particle-containing blood perfusing that tissue. If the number of particles in the tissue sample is determined, and an adequate blood flow reference established, a tissue blood flow can be derived.

Calculating the blood flow rate is straightforward; it is based on the assumption that the number of microspheres in each organ should be directly proportional to blood flow to that organ, e.g.,

\[
\frac{\text{Blood flow to organ A}}{\text{Microspheres in organ A}} = \frac{\text{blood flow to organ B}}{\text{microspheres in organ B}} = \frac{\text{cardiac output}}{\text{total microspheres injected}}
\]  

(2.15)

The cardiac output of the animal is obtained by another independent method.

Like any other experimental method, determination of blood flow by radioactive microspheres is subject to many sources of error, including individual variation among the sample population, the counting accuracy of the total microspheres in the tissue sample by the gamma counter, and the effect of arteriovenous shunting or the migration of the microspheres. Despite all the limitations of this method, the microsphere technique of blood flow determination has become the most powerful method available today and has been used to evaluate the accuracy of other techniques of blood flow measurement.

**Doppler Ultrasound.** Doppler ultrasound has been widely used to provide qualitative measurements of the average flow velocity in large to medium-size vessels if the vessel diameter is known. These include the extracranial circulation and peripheral limb vessels. It is also used in an assessment of mapped occlusive disease of the lower extremities. The frequency used for Doppler ultrasound is typically between 1 and 15 MHz. The basis of this method is the Doppler shift, which is the observed difference in frequency between sound waves that are transmitted from simple piezoelectric transducers and those that are received back when both transmitter and receiver are in relative motion. The average frequency shift of the Doppler spectrum is proportional to the average paniculate velocity over the cross-sectional area of the sample. When used to measure blood flow, the transducers are stationary and motion is imparted by the flowing blood cells. In this event, red cell velocity \( V \) is described by the relationship

\[
\frac{\delta F}{F} = \left( \frac{2V}{C} \right) \cos \theta
\]  

(2.16)

or

\[
V = \frac{\delta F}{F} \left( \frac{C}{2 \cos \theta} \right)
\]  

(2.17)
where $\delta F =$ frequency change of the emitted wave

$C =$ mean propagation velocity of ultrasound within tissues (about 1540 m/s)

$\theta =$ angle between the ultrasound beam and the flow velocity

The frequency shift is usually in the audible range and can be detected by an audible pitch variation or can be plotted graphically.

Attenuation of ultrasound increases nearly linearly with frequency in many types of tissue, causing high frequencies to be attenuated more strongly than low frequencies. The depth of penetration of the signal also depends on the density of the fluid; hence sampling of the velocity profile could be inaccurate in situations where this can vary. Determination of absolute flow/tissue mass with this technique has limited potential, since vessel diameter is not accurately measured and volume flow is not recorded. It is not possible, using currently available systems, to accurately measure the angle made by the ultrasonic beam and the velocity vector. Thus, Doppler flow measurements are semi-quantitative.

**Laser Doppler Flowmetry.** Laser Doppler flowmetry (LDF) offers the potential to measure flow in small regional volumes continuously and with repetitive accuracy. It is ideally suited to measure surface flow on skin or mucosa or following surgical exposure. LDF couples the Doppler principle in detecting the frequency shift of laser light imparted by moving red blood vessels in the blood stream. Incident light is carried to the tissue by fiber optic cables, where it is scattered by the moving red blood cells. By sampling all reflected light, the device can calculate flux of red blood cells within the sample volume. Depending on the light frequency, laser light penetrates tissue to a depth of less than approximately 3 mm.

The output from LDF is measured not in easily interpretable units of flow but rather in hertz. It would be ideal to define a single calibration factor that could be used in all tissues to convert laser output to flow in absolute units. Unfortunately, the calibration to determine an absolute flow is limited by the lack of a comparable standard and the lack of preset controlled conditions. This may be due to varying tissue optical properties affected by tissue density (Obeid et al., 1990). Further, LDF signals can be affected by movement of the probe relative to the tissue.

Despite its limitations, LDF continues to find widespread applications in areas of clinical research because of its small probe size, high spatial and temporal resolution, and entire lack of tissue contact if required. It has been suggested that LDF is well suited for comparisons of relative changes in blood flow during different experimental conditions (Smits et al., 1986). It is especially valuable to provide a direct measurement of cutaneous blood flow. In patients with Raynaud’s phenomenon, it has been indicated that the abnormal cutaneous blood flow is related to the diminished fibrinolytic activity and increased blood viscosity (Engelhart and Kristensen, 1986). LDF has also been useful for assessing patients with fixed arterial obstructive disease of the lower extremity (Schabauer and Rooke, 1994). Other cutaneous uses of LDF include postoperative monitoring of digit reattachment, free tissue flap, and facial operations (Schabauer and Rooke, 1994). In the noncutaneous application of LDF, it has been reported to measure the retinal blood flow in patients with diabetes mellitus. LDF has also been used to monitor cerebral blood perfusion (Borgos, 1996). Recently, it was used to evaluate the brain autoregulation in patients with head injury (Lam et al., 1997).

**Temperature Pulse Decay Technique.** As described in Sec. 2.4 under “Temperature Pulse Decay (TPD) Technique,” local blood perfusion rate can be derived from the comparison between the theoretically predicted and experimentally measured temperature decay of a thermistor bead probe. The details of the measurement mechanism have been described in that section. The temperature pulse decay technique has been used to measure the in vivo blood perfusion rates of different physical or physiological conditions in various tissues (Xu et al., 1991; 1998). The advantages of this technique are that it is fast and induces little trauma. Using the Pennes bioheat transfer equation, the intrinsic thermal conductivity and blood perfusion rate can be simultaneously measured. In some of the applications, a two-parameter least-square residual fit was first performed to obtain the intrinsic thermal conductivity of the tissue. This calculated value of thermal conductivity was then used to
perform a one-parameter curve fit for the TPD measurements to obtain the local blood perfusion rate at the probe location. The error of blood perfusion measurement using the TPD technique is mainly inherited from the accuracy of the bioheat transfer equation. Theoretical study (Xu et al., 1993) has shown that this measurement is affected by the presence of large blood vessels in the vicinity of the thermistor bead probe. Further, poor curve fitting of the blood perfusion rate occurs if the steady state of the tissue temperature is not established before the heating (Xu et al., 1998).

### 2.5 HYPERTERMIA TREATMENT FOR CANCERS AND TUMORS

#### 2.5.1 Introduction

Within the past decade, there have been important advances in the use of hypertermia in a wide variety of therapeutic procedures, especially for cancer treatment. Hypertermia is used either as a singular therapy or as an adjuvant therapy with radiation and drugs in human malignancy. It has less complications and is preferable to more costly and risky surgical treatment (Dewhirst et al., 1997). The treatment objectives of current therapy are to raise tumor temperature higher than 43°C for periods of more than 30 to 60 minutes while keeping temperatures in the surrounding normal tissue below 43°C. It has been suggested that such elevated temperatures may produce a heat-induced cytotoxic response and/or increase the cytotoxic effects of radiation and drugs. Both the direct cell-killing effects of heat and the sensitization of other agents by heat are phenomena strongly dependent on the achieved temperature rise and the heating duration.

One of the problems encountered by physicians is that current hypertermia technology can’t deliver adequate power to result in effective tumor heating of all sites. The necessity of developing a reliable and accurate predictive ability for planning hypertermia protocols is obvious. The treatment planning typically requires the determination of the energy absorption distribution in the tumor and normal tissue and the resulting temperature distribution. The heating patterns induced by various hypertermia apparatus have to be studied to focus the energy on a given region of the body and provide a means for protecting the surrounding normal tissues. Over the past decade, optimization of the thermal dose is possible with known spatial and temporal temperature distribution during the hypertermia treatment. However, large spatial and temporal variations in temperature are still observed because of the heterogeneity of tissue properties (both normal tissue and tumor), spatial variations in specific absorption rates, and the variations and dynamics of blood flow (Overgaard, 1987). It has been suggested that blood flow in large, thermally unequilibrated vessels is the main cause for temperature nonhomogeneity during hypertermia treatment, since these large vessels can produce cold tracts in the heated volume. Thus, to heat the tissue and tumor volume effectively and safely, it is critical to experimentally or theoretically monitor the temporal and spatial temperature gradient during the hypertermia treatment.

#### 2.5.2 Temperature Monitoring during Thermal Treatment

One of the reasons hypertermia has not yet become widely accepted as a mode of therapy is the lack of noninvasive and inexpensive temperature measurement technology for routine use. Invasive temperature devices have a number of restrictions when applied to temperature monitoring during hypertermia. These restrictions include small representative tissue sample of the entire tissue and tumor volume, difficulty in inserting the devices into a deep-seated tumor, and discomfort to patients. Because of the problems associated with invasive temperature measurement techniques, there has been a strong demand for noninvasive temperature feedback techniques such as ultrasonic imaging and microwave radiometry imaging (MRI). In addition to their focusing and real-time capabilities, ultrasound-based techniques are capable of providing satisfactory temperature resolution as well as hot-spot localization in soft tissue. MRI was applied as a noninvasive thermometry method, but it has limited temperature resolution (~0.5°C) and spatial resolution (~1 cm) and therefore can provide only
an estimate of the average temperature over a certain tissue volume. Further, MRI is a costly technique, and therefore, it does not comply with the clinical requirements of treatment monitoring for tissue temperature distribution.

### 2.5.3 Heating Patterns Induced by Hyperthermia Applicators

**Ideal Treatment Volume and Temperature Distribution.** Heating pattern or specific absorption rate (SAR) induced by external devices is defined as the heat energy deposited in the tissue or tumor per second per unit mass or volume of tissue. In optimal treatment planning, it is the temperature rather than the SAR distribution that is optimized in the treatment plan. The maximum temperature generally occurs in the tissue region with heat deposition. However, one should note that SAR and temperature distribution may not have the same profile, since temperature distribution can also be affected by the environment or imposed boundary conditions.

The thermal goal of a clinically practical hyperthermia treatment is to maximize the volume of tumor tissue that is raised to the therapeutic temperature. This maximization should be accomplished while keeping the volume of normal tissue at or below some clinically specific temperature level. There are difficulties to reaching the optimal temperature distribution with the presently available heating devices. Most clinical heating systems have had such fixed power deposition patterns that optimization was limited. In recent years, the cooperation between engineers and clinicians has resulted in a new generation of heating equipment. These heating devices have considerably more flexibility in their ability to deposit power in different patterns that help reach the treatment goal. Further, the ideal temperature distribution may be achieved by manipulating the geometrical consideration or regional blood flow. In most of the transurethral microwave catheters, circulated cold water is installed in the catheter to provide protection to the sensitive prostatic urethra. Manipulation of the flow rate and temperature of the water have been demonstrated to facilitate the achievement of high temperature penetrating deep in the transition zone (Liu et al., 2000). Preheating the large arterial blood to some extent before it enters the treatment region has also been shown to improve the temperature homogeneity in that area.

**Currently Used Heating Devices.** It is known that the size and location of the tumor have a significant impact on applicator design and type of heating. In most of the heating devices, heat is deposited in the tissue via electromagnetic wave absorption (microwave or radio frequency), electric conductive heating, ultrasound absorption, laser, and thermal seed, etc. In this section, different heating devices are introduced and their advantages and limitations are described.

High-energy dc shock (Scheinman et al., 1982) has been used as an implanted energy source for the treatment of drug-refractory supraventricular arrhythmias. During the dc catheter ablation, the peak voltage and current measured at the electrode-tissue interface are typically higher than 1000 V and 40 A, respectively. The high-voltage pulse results in a very high temperature at the electrode surface. Explosive gas formation and a shock wave can occur, which may cause serious complications, including ventricular fibrillation, cardiogenic shock, and cardiac perforation.

Alternating current in the radio-frequency range has been investigated as an alternative to dc shock for heating applicator (Huang et al., 1987; Nath et al., 1994; Nath and Haines, 1995; Wonnell, et al., 1992; Zhu and Xu, 1999). RF energy is readily controllable, and the equipment is relatively cheap. The standard RF generator used in catheter ablation produces an unmodulated sinusoidal wave alternating current at frequency of 200 to 1000 kHz. Two electrodes are needed to attach to the tissue and a current is induced between them. The passage of current through the tissue results in resistive or ohmic heating (FR losses). Resistive current density is inversely proportional to the square of the distance from the electrode. Thus, resistive heating decreases with the distance from the electrode to the fourth power. Maximal power occurs within a very narrow rim of tissue surrounding the electrodes. The heating typically leads to desiccation of tissue immediately surrounding the catheter electrodes, but diverges and decreases in between, which can cause broad variations of heating. Improved RF hyperthermia systems have been proposed to reduce the heterogeneity of the RF heating, including implanting a feedback power current system (Astrahan, 1982; Hartov et al., 1994) and using electrically insulating material around the electrodes (Cosset et al., 1986).
Microwave hyperthermia uses radiative heating produced by high-frequency power. High-frequency electromagnetic waves may be transmitted down an appropriately tuned coaxial cable and then radiated into the surrounding medium by a small antenna. The mechanism of electromagnetic heating from a microwave source is dielectric, rather than ohmic. The heating is due to a propagating electromagnetic wave that raises the energy of the dielectric molecules through which the field passes by both conduction and displacement currents. While maintaining alignment with the alternating electric field, neighboring energized dipole molecules collide with each other and the electromagnetic energy is transformed into kinetic energy (heat). The main limitation of microwave heating is that the energy is absorbed within a very narrow region around the microwave antenna. Typically, the generated heat decays fast and can be approximated as proportional to \(1/r^2\). The highly absorptive nature of the water content of human tissue has limited the penetration of electromagnetic energy to 1 to 2 centimeters.

Laser photocoagulation is a form of minimally invasive thermotherapy in which laser energy is deposited into a target tissue volume through one or more implanted optical fibers. Laser is used in medicine for incision and explosive ablation of tumors and other tissues, and for blood vessel coagulation in various tissues. Laser light is nearly monochromatic. Most popular lasers utilized in the laboratory include Nd:YAG lasers operating at 1064 nm and diode lasers operating at 805 nm. Laser-beam power ranges from milliwatts to several watts. Usually the laser energy is focused on a small tissue area of a radius less than 300 \(\mu\)m, resulting in a very high radiance. Because there is minimal penetration of laser energy into the tissue, sufficient energy is delivered to heat tissues surrounding the point of laser contact to beyond 60°C or higher, leading to denaturation and coagulation of biomolecules. Because of the high temperature elevation in the target tissue, laser photocoagulation may produce vapor, smoke, browning, and char. A char is usually formed when temperature is elevated above 225°C (LeCarpentier et al., 1989; Thomsen, 1991; Torres et al., 1990; Whelan and Wyman, 1999).

Unlike the electromagnetic heating devices mentioned above, ultrasound heating is a mechanical hyperthermic technique. The acoustic energy, when absorbed by tissue, can lead to local temperature rise. Ultrasound offers many advantages as an energy source for hyperthermia because of its small wavelength and highly controllable power deposition patterns, including penetration depth control in human soft tissue. The depth of the resulting lesion could theoretically be increased or decreased by selecting a lower or higher ultrasound frequency, respectively. It has been shown that scanned focused ultrasound provides the ability to achieve more uniform temperature elevations inside tumors than the electromagnetic applicators. Moros and Fan (1998) have shown that the frequency of 1 MHz is not adequate for treating chest wall recurrences, since it is too penetrating. As for deep-seated tumor (3 to 6 cm deep), longer penetration depth is achieved by using relatively low frequency (1 MHz) and/or adjusting the acoustic output power of the transducer [Moros et al., 1996]. The practical problem associated with ultrasound heating is the risk of overheating the surrounding bone/tissue interface because of the high ultrasound absorption in bone.

**Determination of SAR.** Several methods are used to determine the SAR distribution induced by various heating applicators. The SAR distribution can be directly derived from the Maxwell equation of the electromagnetic field (Camart et al., 2000; Gentili et al., 1995; Ling et al., 1999; Stauffer et al., 1998; Strohbehn, 1984). The electrical field \(E\) and magnetic field \(B\) are first determined analytically or numerically from the Maxwell equation. The SAR (W/kg) is then calculated by the following equation (Sapozink et al, 1998):

\[
\text{SAR} = \frac{\sigma \rho E^2}{\sigma^2 \rho}
\]

where \(\rho\) and \(\sigma\) represent the density and conductivity of the media, respectively. This method is feasible when the derivation of the electromagnetic field is not very difficult. It generally requires a rather large computational resource and a long calculation time, though it is flexible for modeling the applicators and the surrounding media.
Other methods in clinical and engineering applications are experimental determination of the SAR distribution based on the heat conduction equation. The experiment is generally performed on a tissue equivalent phantom gel. The applicability of the SAR distribution measured in the phantom gel to that in tissue depends on the electrical properties of the phantom gel. For energy absorption of ultrasound in tissue, the gel mimics tissue in terms of ultrasonic speed and attenuation/absorption properties. For heat pattern induced by microwave or radio frequency, the applicability requires that the phantom gel mimic the dielectric constant and electrical conductivity of the tissue. The electrical properties of various tissues at different wave frequencies have been studied by Stoy et al. (1982). It has been shown that in addition to the electromagnetic wave frequency, water content of the tissue is the most important factor determining the electrical properties. Thermal properties such as heat capacity and thermal conductivity of the gel are not required if no thermal study is conducted. The ingredients of the gel can be selected to achieve the same electrical characteristics of the tissue for a specific electromagnetic wavelength. As shown in Zhu and Xu (1999), the basic ingredients of the gel used for an RF heating applicator were water, formaldehyde solution, gelatin, and NaCl. Water was used to achieve a similar water content as the tissue. Formaldehyde and gelatin were the solidification agents. NaCl was added to obtain the desired electrical conductivity of tissue at that frequency. The resulted phantom gel was a semitransparent material that permits easy and precise positioning of the temperature sensors during the experimental study.

The simplest experimental approach to determining the SAR distribution is from the temperature transient at the instant of power on (Wong et al., 1993; Zhu et al., 1996b). In this approach, temperature sensors are placed at different spatial locations within the gel. Before the experiment, the gel is allowed to establish a uniform temperature distribution within itself. As soon as the initial heating power level is applied, the gel temperature is elevated and the temperatures at all sensor locations are measured and recorded by a computer. The transient temperature field in the gel can be described by the heat conduction equation:

\[
\rho C \frac{\partial T}{\partial t} = k \nabla^2 T + \text{SAR}(x,y,z) \tag{2.19}
\]

At \( t = 0 \), \( T = T_{\text{env}} = \text{constant} \)

Within a very short period after the heating power is on, heat conduction can be negligible if the phantom gel is allowed to reach equilibration with the environment before the heating. Thus, the SAR can be determined by the slope of the initial temperature rise, i.e.,

\[
\text{SAR} = \rho C \left( \frac{\partial T}{\partial t} \right) \bigg|_{t=0} \tag{2.20}
\]

Since the SAR at each spatial location is a constant during the heating, the temperature rise at each location is expected to increase linearly if heat conduction is negligible. Figure 2.5 gives the measured temperature rise at different radial locations from a cylindrical microwave antenna. Note that the temperatures at all three probe locations were very close to each other before the heating. The temperatures increased linearly once the power was on; however, after approximately 60 seconds, the plot became curved and heat conduction within the gel was no longer negligible. For convenience the loose SAR data are generally represented by an analytic expression with several unknown parameters. Then a least-square residual fit of the SAR measurement to the analytical expression is performed to determine the unknown parameters in the expression.

It is simple to determine the SAR distribution from the initial temperature transient. This method is fairly accurate as long as the temperature is uniform before the power is turned on. However, to obtain an accurate expression for the SAR distribution, enough temperature sensors should be placed in the region where the energy is absorbed. In the situation when the SAR decays rapidly in the radial direction because of the superficial penetration of the energy, and it is difficult to place many...
temperature sensors in the near field, the SAR distribution must be determined by only a few measurements in the near field, which increases the measurement error.

In the experimental study by Zhu et al. (1998), the heating pattern induced by a microwave antenna was quantified by solving the inverse problem of heat conduction in a tissue equivalent gel. In this approach, detailed temperature distribution in the gel is required and predicted by solving a two- or three-dimensional heat conduction equation in the gel. In the experimental study, all the temperature probes were not required to be placed in the near field of the catheter. Experiments were first performed in the gel to measure the temperature elevation induced by the applicator. An expression with several unknown parameters was proposed for the SAR distribution. Then, a theoretical heat transfer model was developed with appropriate boundary conditions and initial condition of the experiment to study the temperature distribution in the gel. The values of those unknown parameters in the proposed SAR expression were initially assumed and the temperature field in the gel was calculated by the model. The parameters were then adjusted to minimize the square error of the deviations theoretically predicted from the experimentally measured temperatures at all temperature sensor locations.

2.5.4 Dynamic Response of Blood Flow to Hyperthermia

As mentioned previously, blood flow plays a profound effect in the temperature field during hyperthermia treatment. Accurately measuring and monitoring blood flow in different tissue regions and at different heating levels is especially crucial to achieve the thermal goal. The distribution of blood flow is quite heterogeneous in the tissue. Blood flow rate may be higher in the skin than in the muscle. Blood flow in the tumor and normal tissue may also be quite different because of different vasculatures. Contrary to the general notion that blood flow is less in tumors than in normal tissues, blood flow in many tumors, particularly in small tumors, is actually greater than that in surrounding normal tissues at normothermic conditions. Even in the same tumor, blood flow generally decreases as the tumor grows larger, owing partially to progressive deterioration of vascular beds and to the rapid growth of tumor cell population relative to vascular bed.

The dynamic responses of the blood flow to hyperthermia in normal tissue and tumors are even more diversified than the blood flow heterogeneity. It is a well-known fact that heat induces a prompt
increase in blood flow accompanied by dilation of vessels and an increase in permeability of the vascular wall in normal tissues. The degree of pathophysiological changes in the vascular system in normal tissue is, of course, dependent on the heating temperature, the heating duration, and the heating protocol. Experimental study by Song (1984) has shown how the vasculature changed in the skin and muscle of rodents at different time intervals after hyperthermia for varying heating temperatures at 42 to 45°C. It was shown that the blood flow in the skin increased by a factor of 4 and 6 upon heating at 43°C for 60 and 120 min, respectively. At 44°C the skin blood flow was about 12 times the control value within 30 minutes. At high heating temperature, there existed a critical time after which the blood flow decreased because of vasculature damage. This critical time was more quickly reached when the heating temperature was higher. The blood flow increase in the muscle was similar to that observed in the skin, a tenfold increase in the blood flow was noticed at the 45°C heating.

An indisputable fact emerging from various experimental data indicates that heat-induced change in the blood flow in some tumors is considerably different from that in normal tissue. As noted in Figure 2.6, there was a limited increase in blood flow in tumors during the initial heating period (Song, 1984). When the heating was prolonged, the tumor blood flow decreased progressively. The different responses of the normal tissue and tumors suggest the feasibility of selective tumor heating. A relatively small increase in blood flow in tumors favors retention of heat within the tumor volume, and thus causes greater heat damage. On the other hand, a large blood flow increase in the normal tissue by vascular dilation causes tissue cooling and high survival of cells.

Since blood flow is the major route of heat dissipation during hyperthermia, attempts have been made to modify the vascular responses in tumors and normal tissue to heat (Reinhold and Endrich, 1986; Song, 1991). Decreased tumor perfusion may induce changes in the tumor microenvironment, such as reduced pH and energy supply, and thus enhance the thermal cytotoxicity (Gerweck, 1977; Overgaard, 1976; Song et al., 1994). An injection of hydralazine to dogs was reported to decrease the blood flow by 50 percent in the tumor and increase the blood flow in the underlying muscle by a factor of 3 (Song, 1984). It was demonstrated that the use of vasoactive drugs led to intracellular acidification.

**FIGURE 2.6** Temperature-dependent changes in the relative blood perfusion rates for muscle and animal tumors. [From Song (1984), with permission.]
of the tumor environment (Song et al., 1994). It has been shown that 1 hour after an intravenous or intraperitoneal injection of KB-R8498, the blood flow in the SCK mammary carcinoma tumors of mice was reduced 30 to 60 percent (Griffin et al., 1998; Ohashi et al., 1998). The effect has also been made to induce a blood flow increase in the normal tissue. It was reported that preferentially dilating vessels in normal tissues using a vasodilator such as Na nitroprusside led to shunting of blood away from the tumor, thus reducing the cooling effect of the blood flow in a tumor during local hyperthermia (Jirtle, 1988; Prescott et al., 1992). Not surprisingly, radiation also altered the response of vasculatures to heat. It was reported that irradiation with 2000 R, given 1 hour before heating at 42°C for 30 min, enhanced the heat-induced vascular damage in the cervical carcinoma of hamsters. Another research showed that hyperthermia of 42°C for 1 hour, given several weeks after x-irradiation, enhanced the capacity of blood flow increase in skin and muscle (Song, 1984).

It has been increasingly evident that the response of vascular beds to heat in tumors differs considerably from that in normal tissues. The effective clinical use of hyperthermia depends on a careful application of these biological principles emerging from experimental work. More experimental measurements of temperature response are needed for different tumor types at different ages. It is also important to evaluate the applicability of the dynamic response measured in animal to human subjects. Another issue to be addressed is the hyperthermia-induced blood flow change in drug delivery, since the reduced tumor blood flow may decrease the drug delivered to the tumors.

### 2.5.5 Theoretical Modeling

In treatment planning, quantitative three-dimensional thermal modeling aids in the identification of power delivery for optimum treatment. Thermal modeling provides the clinician with powerful tools that improve the ability to deliver safe and effective therapy, and permits the identification of critical monitoring sites to assess tumor heating as well as to assure patient safety. Thermal modeling maximizes the information content of (necessarily sparse) invasive thermometry. The empirical temperature expression (if it is possible) can be used to develop an on-line reference for monitoring tissue temperatures and building a feedback control of the applied power to avoid overheating in critical tissue areas during the hyperthermia therapy.

Tissue temperature distributions during hyperthermia treatments can be theoretically determined by solving the bioheat transfer equation (continuum model or vascular model), which considers the contributions of heat conduction, blood perfusion, and external heating. In addition to geometrical parameters and thermal properties, the following knowledge must be determined before the simulation. The SAR distribution induced by the external heating device should be determined first. The regional blood perfusion in the tissue and tumor and their dynamic responses to heating are also required. All this information, with appropriate boundary and initial conditions, allows one to calculate the temperature distribution of the tissue.

Analytical solution for the temperature field during the hyperthermia treatment is available for certain tissue geometries (Liu et al., 2000; Zhu and Xu, 1999). In most of the situations, the temperature field is solved by numerical methods because of the irregular tissue geometry and complicated dynamic response of blood flow to heating (Chatterjee and Adams, 1994; Charny et al., 1987; Clegg and Roamer, 1993).

Parametric studies can be performed to evaluate the influence of different parameters, such as heating level, tissue perfusion, and cooling fluid, on the temperature elevation. Extensive parametric studies can be performed quickly and inexpensively so that sensitive (and insensitive) parameters can be identified, systems can be evaluated, and critical experiments can be identified. This is especially important when the parameter is unknown. It is also possible to extract the ideal SAR distribution from the parametric study (Loulou and Scott, 2000) and design an improved heating applicator in the future. Knowledge of the expected thermal profiles could be used to guide experimental and clinical studies in using an optimum thermal dose to achieve a desired therapeutic effect. The optimal thermal dose needed in the treatment volume predicted by the theory helps physicians evaluate the effectiveness of the heating devices and their treatment protocols.
REFERENCES


