

2.3

$$\frac{G(s)}{s} = \frac{1}{s(s+1)}$$

$$\begin{aligned} G(z) &= \frac{z-1}{z} \cdot \frac{G(s)}{s} \\ &= \frac{0,6321}{z - 0,3679} \end{aligned}$$

$$\begin{aligned} Y(z) &= G(z) \cdot X(z) \\ &= \frac{0,6321z}{(z-1)(z-0,3679)} \\ &= \frac{0,6321z}{z^2 - 1,3679z + 0,3679} \end{aligned}$$

$$Y(z) = 0,6321z^{-1} + 0,8647z^{-2} + 0,9502z^{-3} + 0,9816z^{-4} + 0,9932z^{-5}$$

2.4

$$G(z) = \frac{0,6321z}{z - 0,3679} \quad ; \quad z$$

$$G(z) = \frac{0,6321z^{-1}}{1 - 0,3679z^{-1}} = \frac{Y(z)}{X(z)}$$

$$Y(z) - 0,3679z^{-1}Y(z) = 0,6321z^{-1}X(z)$$

$$Y(z) = 0,6321z^{-1}X(z) + 0,3679z^{-1}Y(z)$$

$$z^{-1}$$

$$\Rightarrow y(k) = 0,6321x(k-1) + 0,3679y(k-1)$$

$$x(k) = \begin{cases} 0, & k < 0 \\ 1, & k \geq 0 \end{cases}$$

k	x(k)	y(k)
0	1	0
1	1	0,6321
2	1	$0,6321 + 0,3679(0,6321) = 0,8646$
3	1	$0,6321 + 0,3679(0,8646) = 0,9502$
4	1	$0,6321 + 0,3679(0,9502) = 0,9816$
5	1	$0,6321 + 0,3679(0,9816) = 0,9932$