

$$\text{Definisi: } e^x = 1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \dots + \frac{1}{n!}x^n + \dots$$

$$x=1 \rightarrow e = e^1 = 1 + 1 + \frac{1}{2} + \frac{1}{6} + \frac{1}{24} + \frac{1}{120} + \dots$$

$$x(t) = X_0 e^{at} = X_0 \left(1 + at + \frac{1}{2}a^2 t^2 + \frac{1}{6}a^3 t^3 + \frac{1}{24}a^4 t^4 + \dots \right)$$

$$\frac{dx(t)}{dt} = X_0 \left(a + a^2 t + \frac{1}{2}a^3 t^2 + \frac{1}{6}a^4 t^3 + \dots \right)$$

$$= a X_0 \left(1 + at + \frac{1}{2}a^2 t^2 + \frac{1}{6}a^3 t^3 + \dots \right)$$

$$= \underbrace{a X_0 e^{at}}_{\text{kembali ke pers. diff}} = a x(t) \rightarrow \text{kembali ke pers. diff}$$

Jadi terbukti bahwa $x(t) = X_0 e^{at}$ adalah

SOLUSI dari pers. diff. $\frac{dx(t)}{dt} = ax(t)$

Bgm kalau $x(t)$: vektor $n \times 1$
dan A : matriks $(n \times n)$